

# MPI Basics

S. Van Crielkingen  
UPJV / MeCS

[www.mecs.u-picardie.fr](http://www.mecs.u-picardie.fr)

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# MPI: references

Official website and specifications :

<http://www mpi-forum.org/>

<http://www mpi-forum.org/docs/mpi-3.0/mpi30-report.pdf>

Tutorials:

<https://computing.llnl.gov/tutorials/mpi/>

[http://www.idris.fr/data/cours/parallel/mpi/choix\\_doc.html](http://www.idris.fr/data/cours/parallel/mpi/choix_doc.html)

[http://www.crihan.fr/calcul/tech/doc\\_ibm\\_pwr5/EchMsg](http://www.crihan.fr/calcul/tech/doc_ibm_pwr5/EchMsg)

[http://www.crihan.fr/calcul/tech/documentation-ibm-cluster-idataplex-antares/formations/OpenMP\\_MPI.zip/view](http://www.crihan.fr/calcul/tech/documentation-ibm-cluster-idataplex-antares/formations/OpenMP_MPI.zip/view)

# Layout

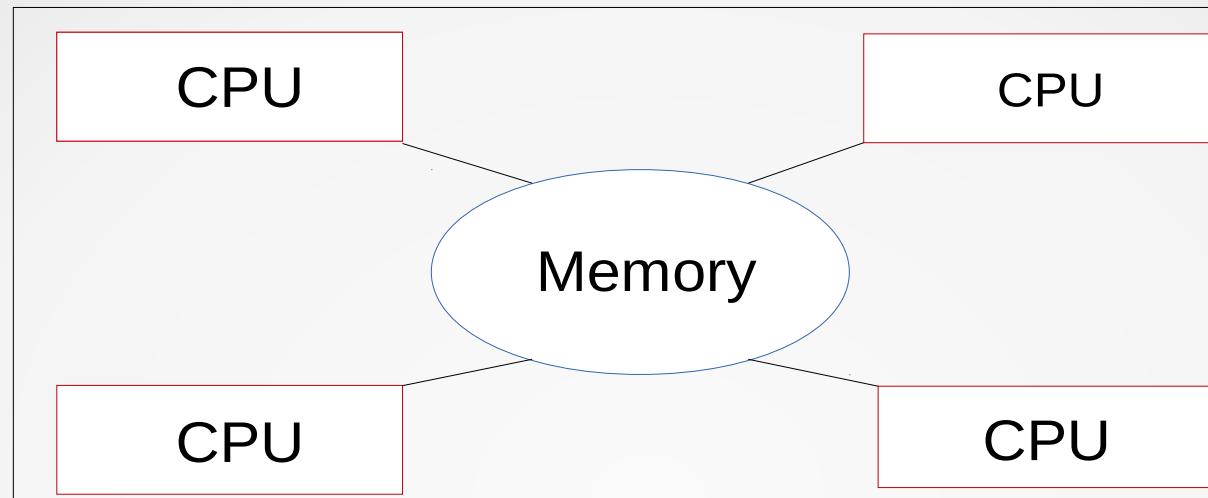
- Introduction & “Hello World”
- Point-to-point Communications
- Collective Communications
- Derived Data Types
- Communicators and Topologies
- Exercises

# Layout

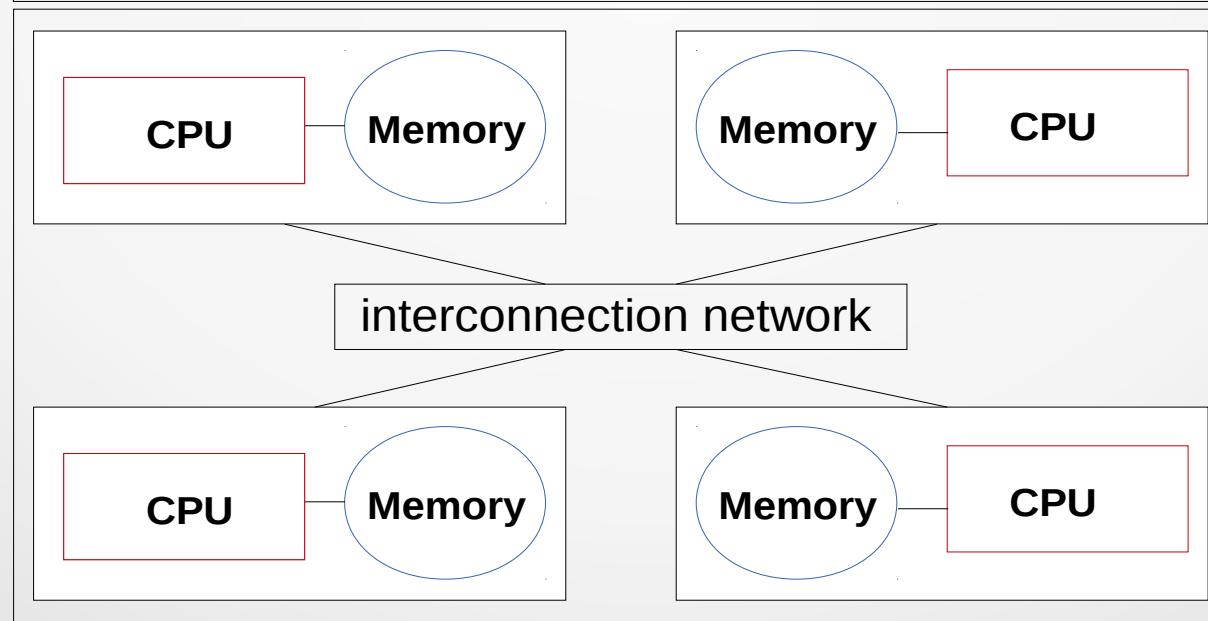
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# Shared vs. Distributed Memory

**Shared**



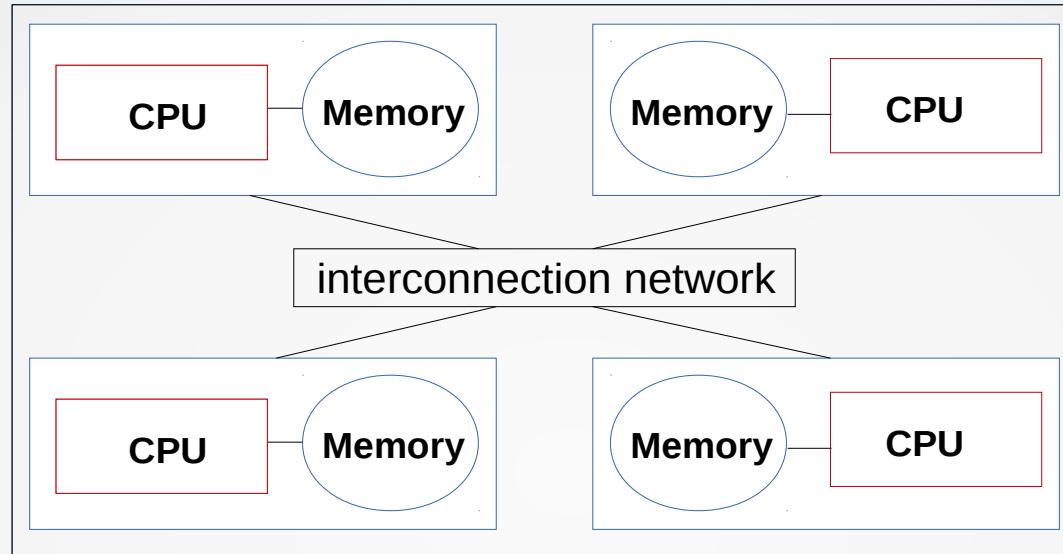
**Distributed**



# Programming models

- For shared memory: multi-threading (e.g. OpenMP)
- For distributed memory: message passing (e.g. MPI)

# Message Passing (distributed memory)



Several processes act each on their own data and memory (own part of **distributed memory**).

Inter-process messages necessary for data exchange and synchronization.

# The MPI standard

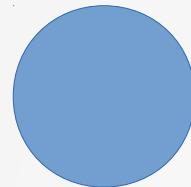
- MPI = Message Passing Interface
- First specification of standard: 1994  
Current version : MPI-3.0 (see MPI Forum)
- Various implementations:  
MPICH, MVAPICH, OpenMPI,...
- Note: MPI also works on shared-memory systems (but OpenMP might be easier to use on such systems).

# MPI: basic principle

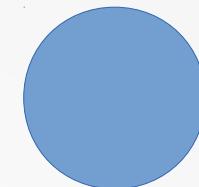
- A (single) MPI program runs on different processor cores, yielding different "MPI processes" or "MPI tasks".
- Each process/task is identified by a **rank** :  
**rank = 0,1, ... ntasks – 1**  
where typically the number of tasks  
ntasks = number of available processor cores.

# MPI: basic principle

Rank = 0

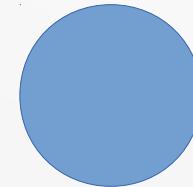


Rank = 1



**ntasks = 3**

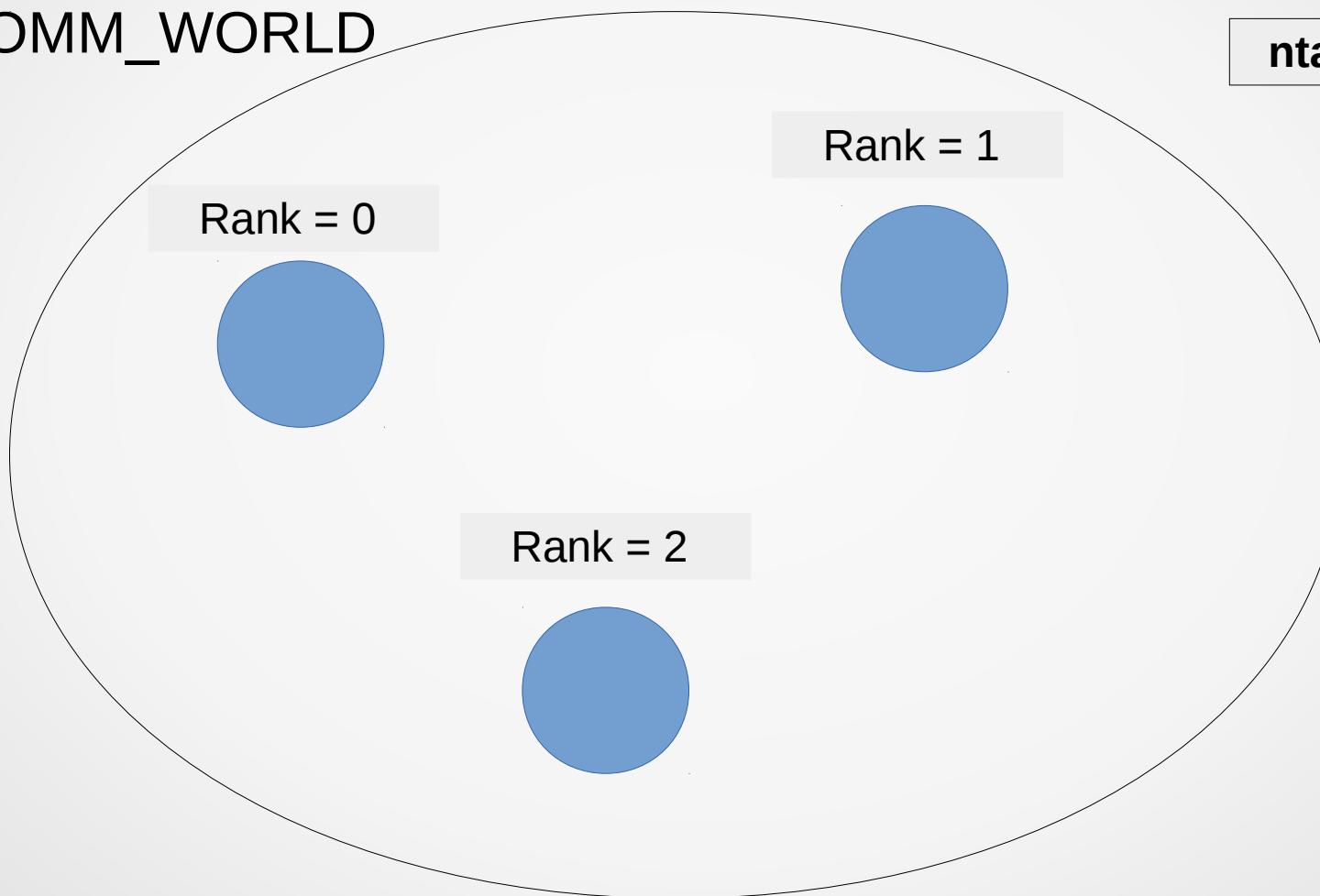
Rank = 2



# MPI: basic principle

`MPI_COMM_WORLD`

`ntasks = 3`



# "Hello world" example (in C)

```
#include "mpi.h"
```

```
#include <stdio.h>
```

```
int main(int argc, char *argv[ ]) {
```

```
    int ntasks, rank;
```

```
    MPI_Init(&argc,&argv);
```

```
    MPI_Comm_size(MPI_COMM_WORLD,&ntasks);
```

```
    MPI_Comm_rank(MPI_COMM_WORLD,&rank);
```

```
    printf ("Hello from rank %d out of %d tasks \n", rank, ntasks);
```

```
    MPI_Finalize();
```

```
}
```

helloWorld.c

*MPI statements  
between ***MPI\_Init***  
and ***MPI\_Finalize****

***MPI\_COMM\_WORLD*** =  
*predefined communicator*  
*including all processes*

```
> mpicc helloWorld.c
```

```
> mpirun -np 3 ./a.out
```

Hello from rank 2 out of 3 tasks

Hello from rank 0 out of 3 tasks

Hello from rank 1 out of 3 tasks

← set number of tasks to 3

Order not deterministic

# MPI: compile and run

Procedure to compile and run a MPI program:

1. To compile: here we use

- **mpicc program.c**
  - **mpif90 program.f90**
- ***a.out*** executable

2. To run on N processors:

- **mpirun -np N ./*a.out***      (or **mpiexec**)

# "Hello world" example (in Fortran 90)

```
program main
```

helloWorld.f90

```
use mpi
```

```
implicit none
```

```
Integer :: ntasks, rank, ierr
```

```
call MPI_INIT(ierr)
```

```
call MPI_COMM_SIZE(MPI_COMM_WORLD, ntasks, ierr)
```

```
call MPI_COMM_RANK(MPI_COMM_WORLD, rank, ierr)
```

```
write(*,'(a,i2,a,i2,a)') 'Hello from rank ', rank, ' out of ',ntasks,' tasks.'
```

```
call MPI_FINALIZE(ierr)
```

```
end
```

```
> mpif90 helloWorld.f90
```

```
> mpirun -np 3 ./a.out
```

Hello from rank 2 out of 3 tasks.

Hello from rank 0 out of 3 tasks.

Hello from rank 1 out of 3 tasks.

← set number of tasks to 3

Order not deterministic

# Main Environment Management Routines

C	Fortran	
<b>MPI_Init</b> (&argc,&argv)	<b>MPI_INIT</b> (ierr)	
<b>MPI_Comm_size</b> (comm,&size)	<b>MPI_COMM_SIZE</b> (comm,size,ierr)	Returns size = number of tasks
<b>MPI_Comm_rank</b> (comm,&rank)	<b>MPI_COMM_RANK</b> (comm,rank,ierr)	Returns rank in [0, size-1]
<b>MPI_Finalize</b> ()	<b>MPI_FINALIZE</b> (ierr)	

where *comm* = communicator = **MPI\_COMM\_WORLD** (typically)

# Main Environment Management Routines

Also useful:

C	Fortran	
<b>MPI_Wtime ()</b>	<b>MPI_WTIME ()</b>	Timing routine
<b>MPI_Abort (comm,errorcode)</b>	<b>MPI_ABORT (comm,errorcode,ierr)</b>	Terminates (all) processes

where *comm* = communicator = MPI\_COMM\_WORLD (typically)

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# Send / Receive

Messages can be sent from one MPI process (rank) to another, which should be ready to receive it

→ an operation between two processes is **cooperative**.

Rank  $n_1$  : **MPI\_Send** (&send\_msg, ..., dest =  $n_2$ , ...)

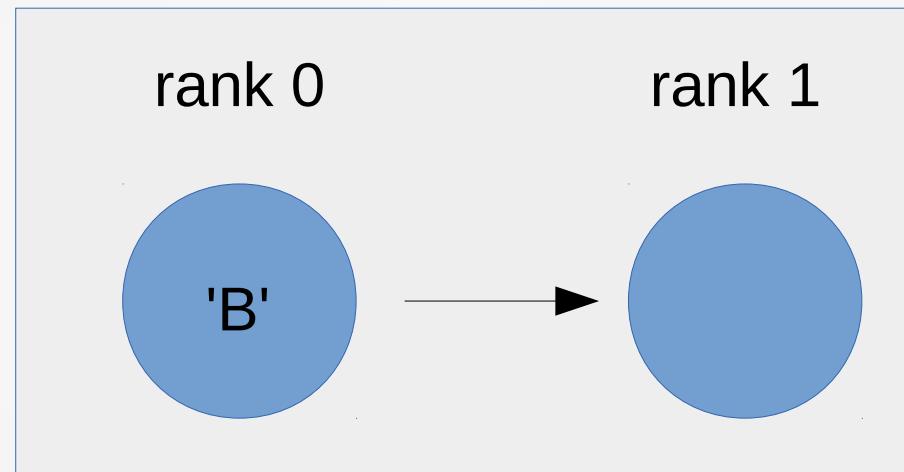


C code

Rank  $n_2$  : **MPI\_Recv** (&recv\_msg, ..., source =  $n_1$ , ...)

N.B. : Since MPI 2.0, there exist *one-sided* communications.

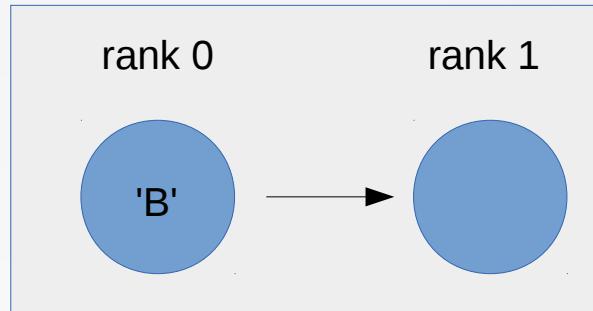
# Send/Receive example



# Send/Receive example (in C, zoom)

[...]

```
count = 1, tag = 1
if (rank == 0) {
    dest = 1;
    sent_msg = 'B';
    MPI_Send (&sent_msg, count, MPI_CHAR, dest, tag, MPI_COMM_WORLD);
    printf("Char sent by rank 0: %c \n", sent_msg);
}
else if (rank == 1) {
    source = 0;
    MPI_Recv (&recv_msg, count, MPI_CHAR, source, tag, MPI_COMM_WORLD, &Stat );
    printf("Char received by rank 1: %c \n", recv_msg);
}
[...]
```

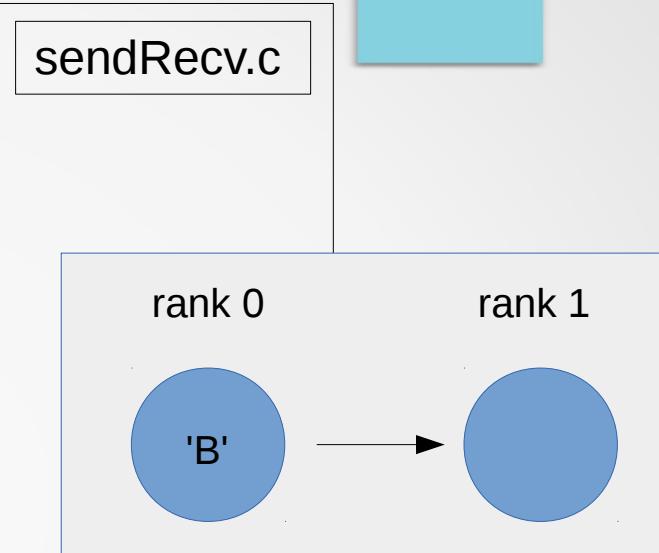


sendRecv.c

```
> mpirun -np 2 ./a.out
Char sent by rank 0: B
Char received by rank 1: B
```

# Send/Receive example (in C)

```
Int main(int argc, char *argv[]) {
    int ntasks, rank, dest, source, count, tag;
    char recv_msg, sent_msg;
    MPI_Status Stat;
    MPI_Init(&argc,&argv);
    MPI_Comm_size(MPI_COMM_WORLD, &ntasks);
    MPI_Comm_rank(MPI_COMM_WORLD, &rank);
    count = 1, tag = 1 ;
    if (rank == 0) {
        dest = 1;
        sent_msg = 'B';
        MPI_Send (&sent_msg, count, MPI_CHAR, dest, tag, MPI_COMM_WORLD);
        printf("Char sent by rank 0: %c \n", sent_msg);
    }
    else if (rank == 1) {
        source = 0;
        MPI_Recv (&recv_msg, count, MPI_CHAR, source, tag, MPI_COMM_WORLD, &Stat );
        printf("Char received by rank 1: %c \n", recv_msg);
    }
    MPI_Finalize();
}
```



```
> mpirun -np 2 ./a.out
Char sent by rank 0: B
Char received by rank 1: B
```

# Send/Receive (in C)

**MPI\_Send (&send\_msg, count, datatype, dest, tag, comm)**

**MPI\_Recv (&recv\_msg, count, datatype, source, tag, comm, &status)**

- **send\_msg / recv\_msg** = message sent / received (passed by reference)
- **count** = number of data elements sent/received
- **datatype** = type of the sent/received data  
In C, this is typically: **MPI\_CHAR**, **MPI\_INT**, **MPI\_FLOAT**...
- **dest/source** = rank of the destination/source

# Send/Receive (in C)

**MPI\_Send (&send\_msg, count, datatype, dest, tag, comm)**

**MPI\_Recv (&recv\_msg, count, datatype, source, tag, comm, &status)**

- **tag** = non-negative integer to identify the message.  
Tag in corresponding **MPI\_Send** and **MPI\_Recv** *must* match.
- **comm** = communicator (typically **MPI\_COMM\_WORLD**)
- **status** = information on received message

**N.B. :** *source + destination + tag + communicator = "message enveloppe"*

# Send/Receive : C vs. Fortran

C code :

**MPI\_Send (&send\_msg, count, datatype, dest, tag, comm)**

**MPI\_Recv (&recv\_msg, count, datatype, source, tag, comm, &status)**

Fortran code :

**MPI\_SEND (send\_msg, count, datatype, dest, tag, comm, ierr)**

**MPI\_RECV (recv\_msg, count, datatype, source, tag, comm, status, ierr)**

C data types	Fortran data types
<b>MPI_CHAR</b>	<b>MPI_CHARACTER</b>
<b>MPI_INT</b>	<b>MPI_INTEGER</b>
<b>MPI_FLOAT</b>	<b>MPI_REAL</b>
<b>MPI_DOUBLE</b>	<b>MPI_DOUBLE_PRECISION</b>
...	...

# Send/Receive example (in Fortran 90)

[...]

```
integer :: ntasks, rank, ierr, dest, source, count = 1, tag = 1
character :: recv_msg, sent_msg
Integer :: Stat(MPI_Status_size)
call MPI_INIT(ierr)
call MPI_COMM_SIZE(MPI_COMM_WORLD, ntasks, ierr)
call MPI_COMM_RANK(MPI_COMM_WORLD, rank, ierr)
if (rank .eq. 0) then
    dest = 1
    sent_msg = 'B'
    call MPI_Send(sent_msg, 1, MPI_CHARACTER, dest, tag, MPI_COMM_WORLD, ierr)
    Write(*,*) 'Char sent by rank 0: ', sent_msg
else if (rank .eq. 1) then
    source = 0
    call MPI_Recv(recv_msg, 1, MPI_CHARACTER, source, tag, MPI_COMM_WORLD, Stat, ierr)
    Write(*,*) 'Char received by rank 1: ', recv_msg
endif
call MPI_FINALIZE(ierr)
end
```

sendRecv.f90

```
> mpirun -np 2 ./a.out
Char sent by rank 0: B
Char received by rank 1: B
```

# Blocking vs. Non-blocking

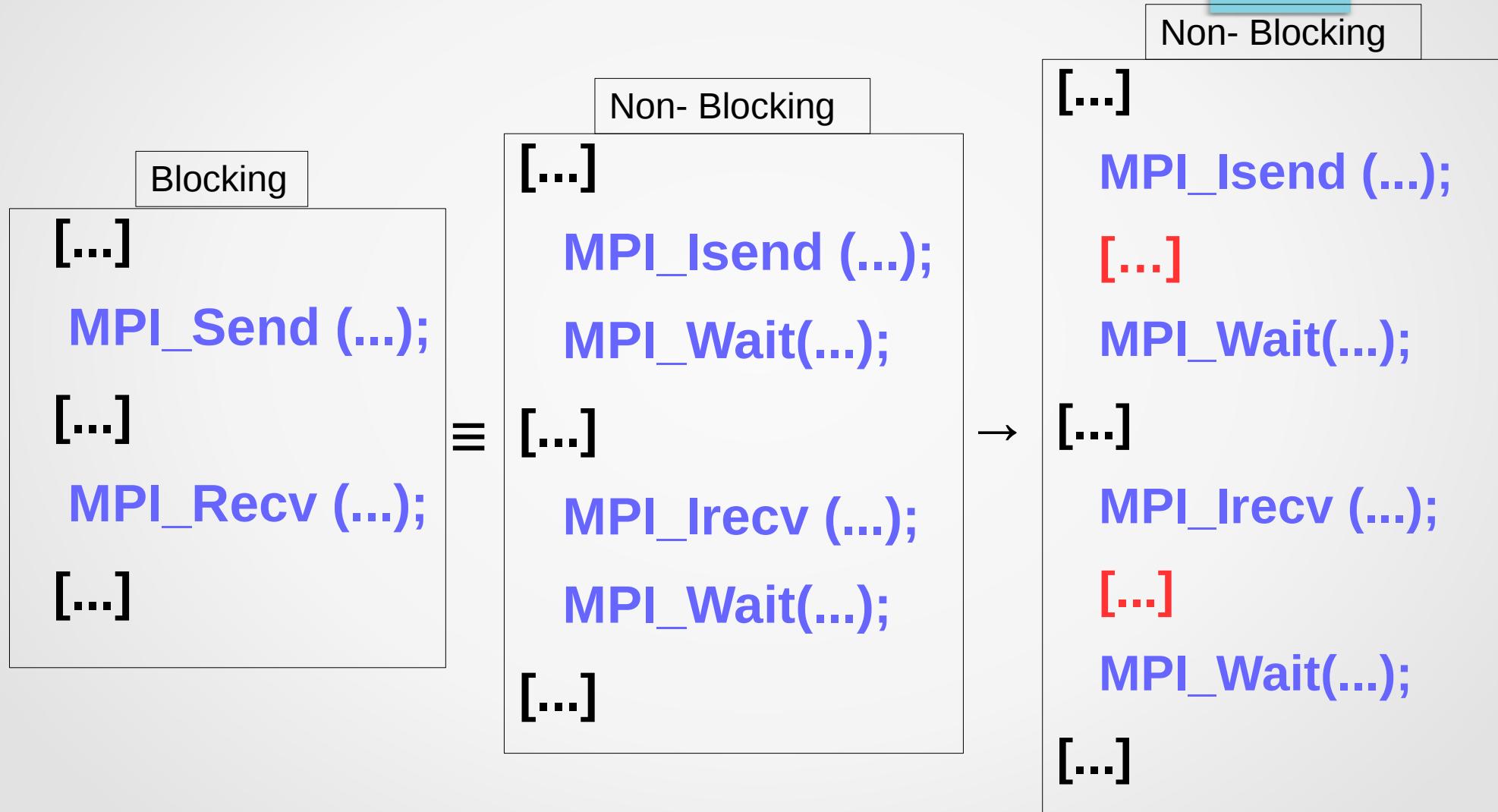
`MPI_Send` / `MPI_Recv` are **blocking** operations: they return only when

- the sent data can be modified
- the received data is ready for use

On the opposite, equivalent **non-blocking** operations `MPI_Isend` / `MPI_Irecv` simply **request** the MPI library to perform the operation when it is able.

The user can not predict when that will happen, but can make sure it happened with a "**wait**" statement.

# Blocking vs. Non-blocking Send/Receive



→ Possibility to overlap communications and computations.

# Blocking vs. Non-blocking Send/Receive

Blocking :

C code

**MPI\_Send (&send\_msg, count, datatype, dest, tag, comm)**

**MPI\_Recv (&recv\_msg, count, datatype, source, tag, comm, &status)**

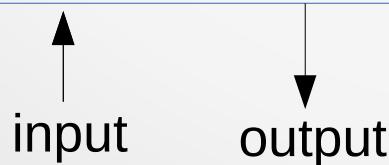
Non-Blocking :

**MPI\_Isend (&send\_msg, count, datatype, dest, tag, comm, &request)**

**MPI\_Irecv (&recv\_msg, count, datatype, source, tag, comm, &request)**

where **request** is an output argument used to determine completion of the non-blocking operation using **MPI\_Wait** :

**MPI\_Wait (&request,&status)**



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# Collective Communications

Opposite to point-to-point communications, collective communications **involve all processes in the communicator** (typically MPI\_COMM\_WORLD).

Types of collective communications:

- Synchronization: barrier
- Data movement: broadcast, scatter, gather
- Reductions

# Synchronization

**MPI\_Barrier (MPI\_COMM\_WORLD)**

C code

**call MPI\_BARRIER (MPI\_COMM\_WORLD, ierr)**

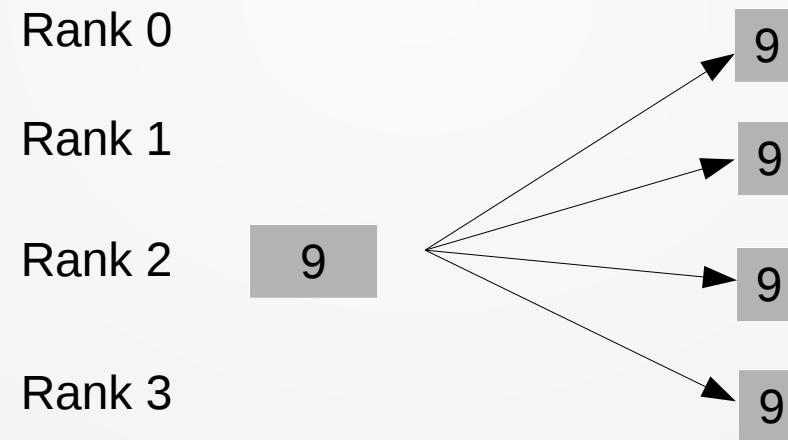
Fortran code

At the barrier, each task blocks until all the other tasks reach the same barrier.

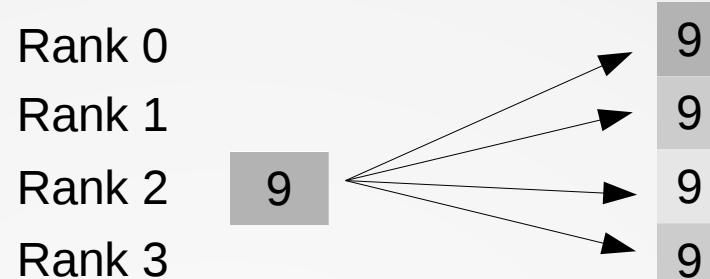
Then all tasks are free to proceed.

# Broadcast

**MPI\_Bcast**



# Broadcast



[...]

```
int msg[1];
source = 2;
count = 1;
if (rank == source){
    msg[0]= 9;
}
MPI_Bcast(&msg, count, MPI_INT, source, MPI_COMM_WORLD);
printf("On rank %d received: %d \n",rank,msg[0]);
MPI_Finalize();
```

C code

```
> mpirun -np 4 ./a.out
On rank 0 received: 9
On rank 1 received: 9
On rank 2 received: 9
On rank 3 received: 9
```

# Broadcast

**MPI\_Bcast** (&msg, count, datatype, source, comm)

C code

- **msg** = message broadcasted
- **count** = number of data elements broadcasted
- **datatype** = type of the broadcasted data
- **source** = rank of the source
- **comm** = communicator (typically MPI\_COMM\_WORLD)

# Scatter

**MPI\_Scatter**

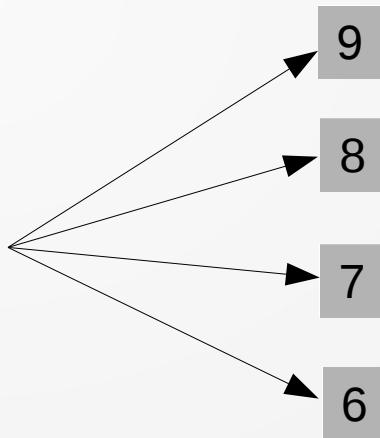
Rank 0

Rank 1

Rank 2

Rank 3

9    8    7    6



# Scatter

```
[...]
int send_msg[4];
int recv_msg[1];
source = 2;
count = 1;
if (rank==source)
{
    send_msg[0] = 9;
    send_msg[1] = 8;
    send_msg[2] = 7;
    send_msg[3] = 6;
}
MPI_Scatter(&send_msg, count, MPI_INT, &recv_msg, count, MPI_INT, source, MPI_COMM_WORLD);
printf("On rank= %d received: %d \n",rank,recv_msg[0]);
MPI_Finalize();
```

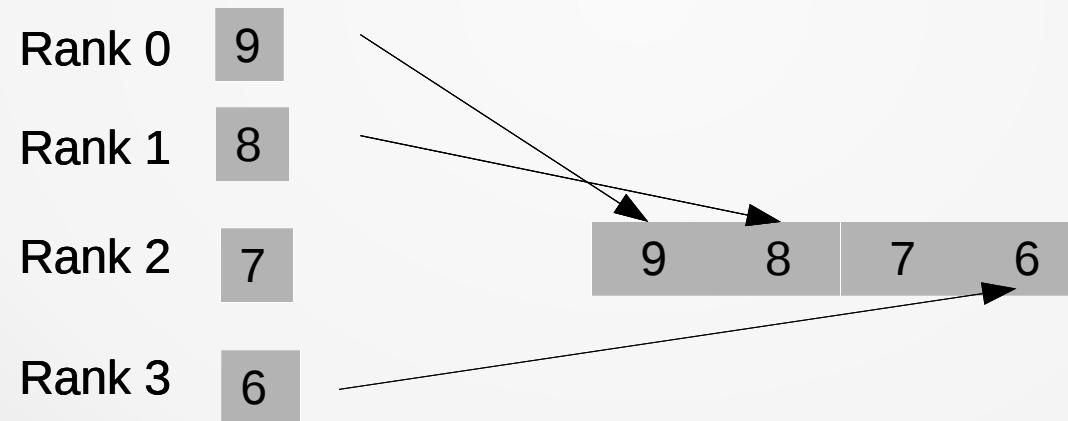
C code



```
> mpirun -np 4 ./a.out
On rank= 0 received: 9
On rank= 1 received: 8
On rank= 2 received: 7
On rank= 3 received: 6
```

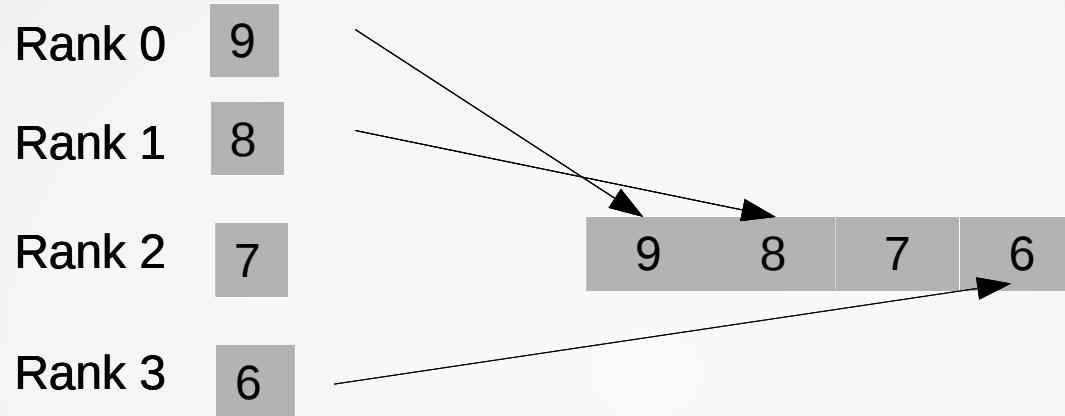
# Gather

**MPI\_Gather**



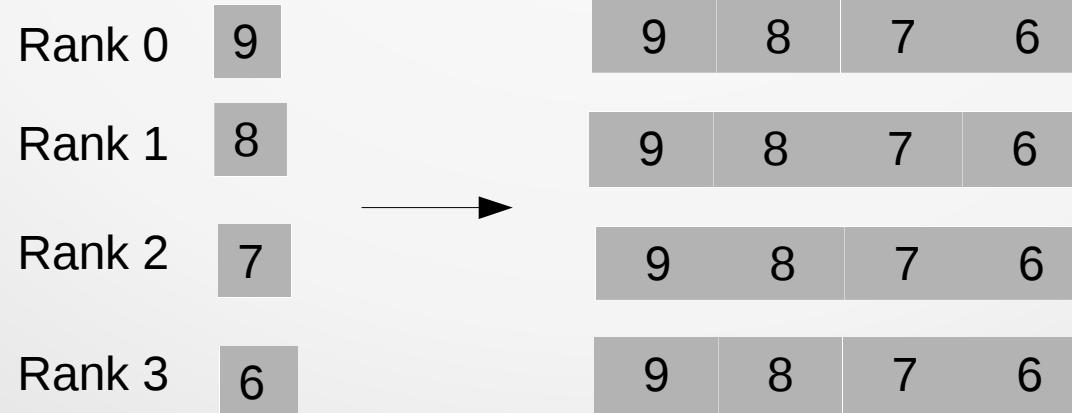
# Note: Gather / AllGather

## MPI\_Gather



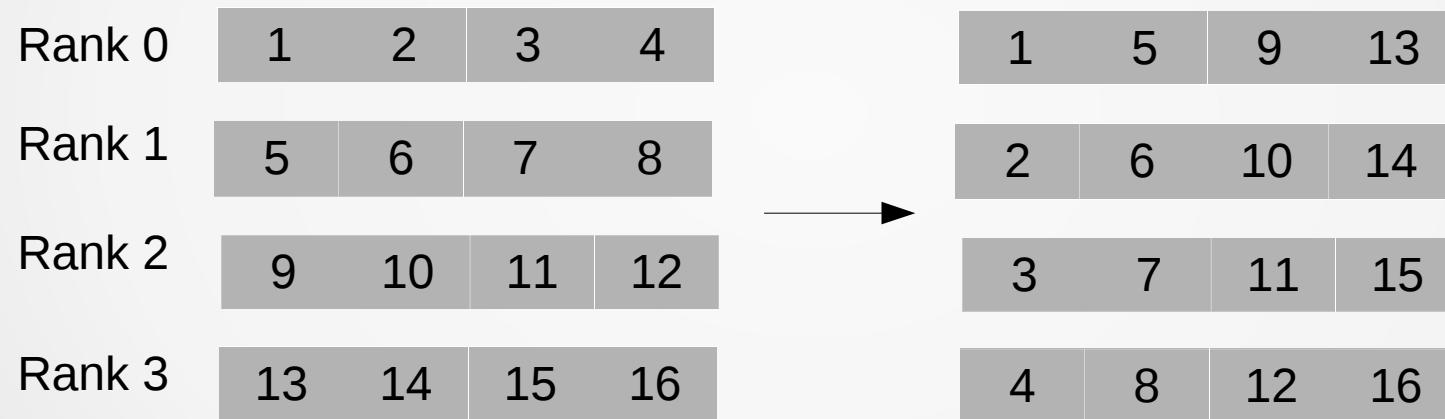
## MPI\_AllGather

"MPI\_AllGather = MPI\_Gather + MPI\_Bcast"



# Note: All to All

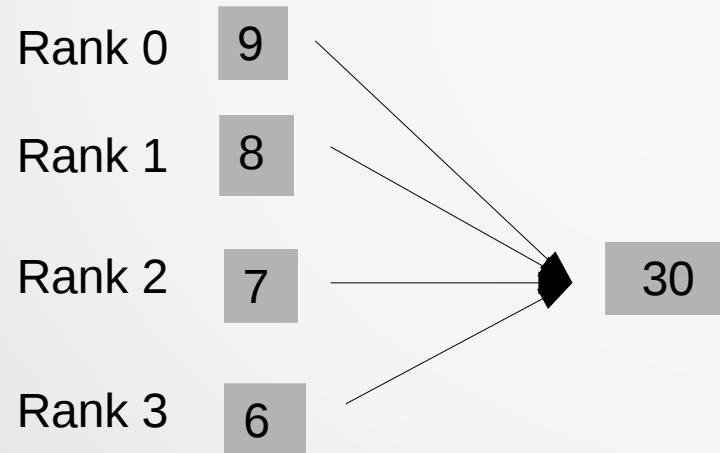
## MPI\_Alltoall



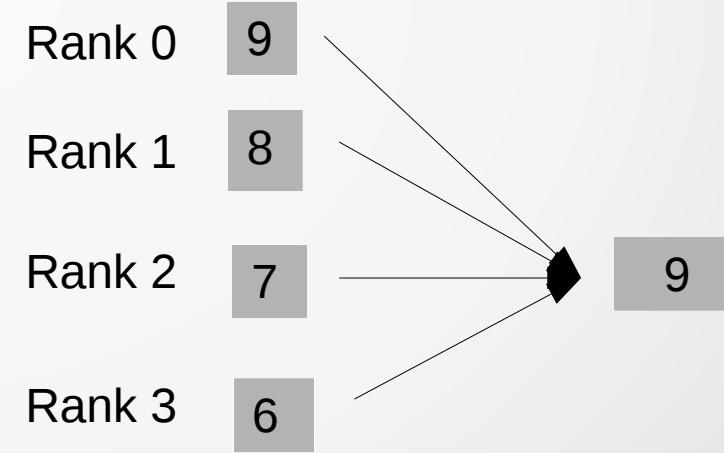
# Reduce

**MPI\_Reduce (... , operator, ...)**

operator = MPI\_SUM



operator = MPI\_MAX

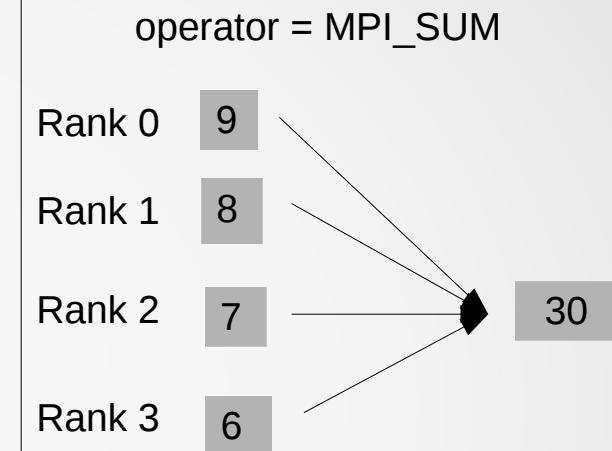


# Reduce

[...]

C code

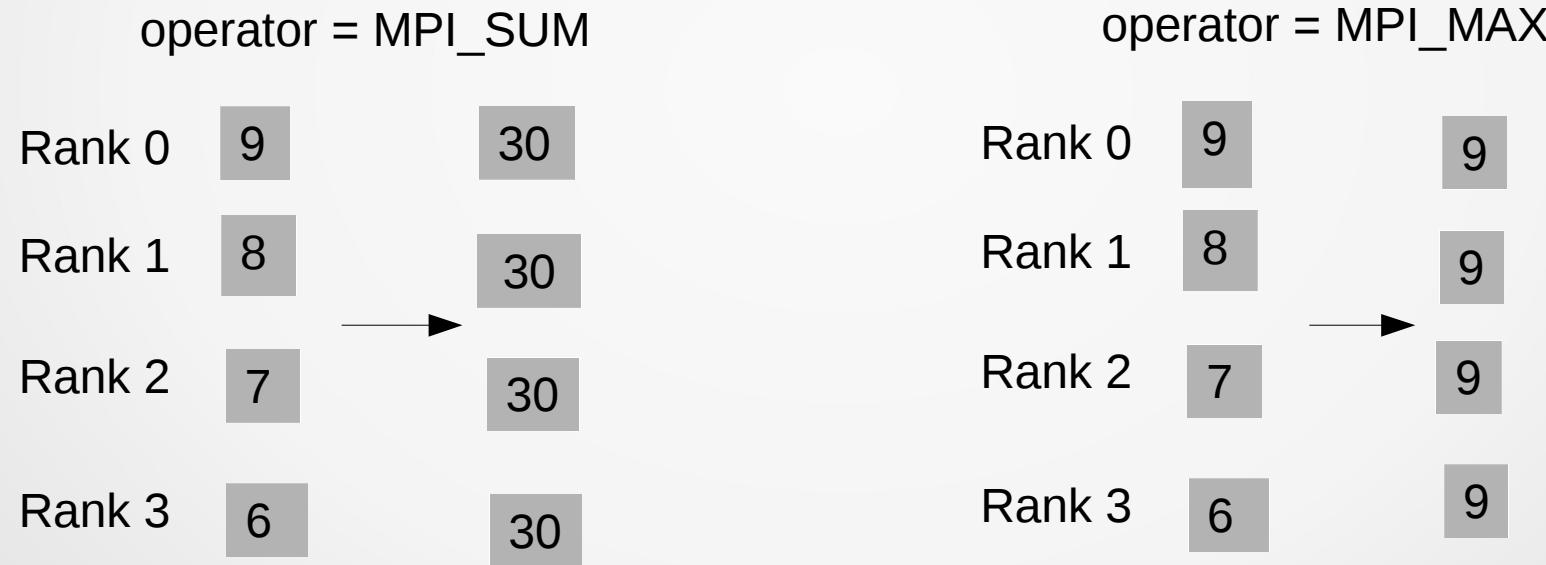
```
int send_msg[1];
int recv_msg[1];
dest = 2;
if (rank==0) send_msg[0] = 9;
if (rank==1) send_msg[0] = 8;
if (rank==2) send_msg[0] = 7;
if (rank==3) send_msg[0] = 6;
MPI_Reduce(&send_msg, &recv_msg, 1, MPI_INT, MPI_SUM, dest, MPI_COMM_WORLD);
if (rank == dest) printf("On rank %d received: %d \n", rank, recv_msg[0]);
MPI_Finalize();
```



```
> mpirun -np 4 ./a.out
On rank 2 received: 30
```

# All Reduce

**MPI\_Allreduce (... , operator, ...)**

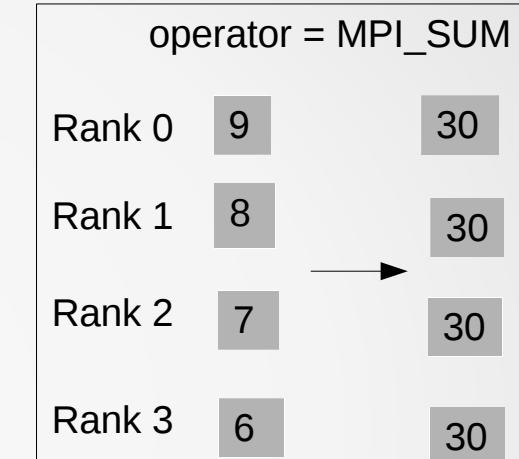


"MPI\_Allreduce = MPI\_Reduce + MPI\_Bcast"

# All Reduce

```
[...]
int send_msg[1];
int recv_msg[1];
MPI_Init(&argc,&argv);
[...]
if (rank==0) send_msg[0] = 9;
if (rank==1) send_msg[0] = 8;
if (rank==2) send_msg[0] = 7;
if (rank==3) send_msg[0] = 6;
MPI_Allreduce(&send_msg,&recv_msg,1,MPI_INT,MPI_SUM,MPI_COMM_WORLD);
printf("On rank= %d received: %d \n",rank,recv_msg[0]);
MPI_Finalize();
```

C code

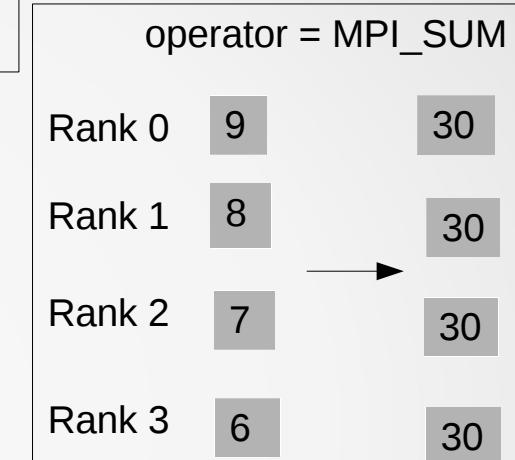


```
> mpirun -np 4 ./a.out
On rank= 0 received: 30
On rank= 1 received: 30
On rank= 2 received: 30
On rank= 3 received: 30
```

# All Reduce

```
[...]  
integer, dimension(1) :: send_msg, recv_msg  
call MPI_Init(ierr)  
[...]  
if (rank==0) send_msg(1) = 9  
if (rank==1) send_msg(1) = 8  
if (rank==2) send_msg(1) = 7  
if (rank==3) send_msg(1) = 6  
call MPI_Allreduce(send_msg,recv_msg,1,MPI_INTEGER,MPI_SUM, MPI_COMM_WORLD,ierr)  
write(*,'(a,i2,a,i2)') 'On rank ', rank, ' received: ', recv_msg(1)  
call MPI_Finalize();
```

Fortran 90 code



```
> mpirun -np 4 ./a.out  
On rank= 0 received: 30  
On rank= 1 received: 30  
On rank= 2 received: 30  
On rank= 3 received: 30
```

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# Primitive vs. Derived Data types

Recall the (primitive) data types usable in MPI communications:

C data types	Fortran data types
MPI_CHAR	MPI_CHARACTER
MPI_INT	MPI_INTEGER
MPI_FLOAT	MPI_REAL
MPI_DOUBLE	MPI_DOUBLE_PRECISION
...	...

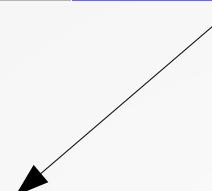
More complex data types can be exchanged with MPI: these are the **Derived Data Types**.

These are typically used to exchange data extracted from existing vectors and matrices.

# MPI\_Type\_contiguous

On rank 0 : a = 

1.0	2.0	3.0	4.0	5.0	6.0	7.0	8.0	9.0
-----	-----	-----	-----	-----	-----	-----	-----	-----



On rank 1 : b = 

3.0	4.0	5.0
-----	-----	-----

**MPI\_Type\_contiguous (n\_extracted, basictype, &newType)**

C code

- **n\_extracted = 3**
  - **basicType = MPI\_FLOAT**
- "newType" generated

# MPI\_Type\_contiguous

[...]

```
float a[9] = {1.0, 2.0, 3.0, 4.0, 5.0, 6.0, 7.0, 8.0, 9.0};  
int n_extracted = 3;  
float b[n_extracted];  
MPI_Datatype newType;  
MPI_Type_contiguous (n_extracted, MPI_FLOAT, &newType);
```

```
MPI_Type_commit(&newType);
```

```
if (rank == 0) {
```

```
    dest = 1;
```

```
    MPI_Send(&a[2], 1, newType, dest, tag, MPI_COMM_WORLD);
```

```
}
```

```
else if (rank == 1) {
```

```
    source = 0;
```

```
    MPI_Recv(b, n_extracted, MPI_FLOAT, source, tag, MPI_COMM_WORLD, &stat);
```

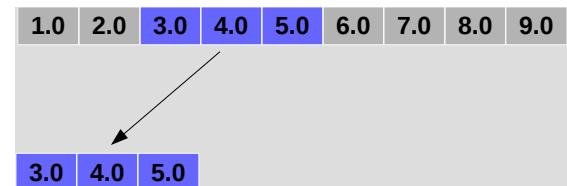
```
    for (i=0;i<n_extracted;++i) printf("On rank %d b[%d]= %2.1f \n", rank, i, b[i]);
```

```
}
```

```
MPI_Type_free(&newType);
```

[...]

DdtContiguous1D.c



```
> mpirun -np 2 ./a.out  
On rank 1 b[0]= 3.0  
On rank 1 b[1]= 4.0  
On rank 1 b[2]= 5.0
```

# MPI\_Type\_contiguous

[...]

```
float a[9] = {1.0, 2.0, 3.0, 4.0, 5.0, 6.0, 7.0, 8.0, 9.0};  
int n_extracted = 3;  
float b[n_extracted];  
MPI_Datatype newType;  
MPI_Type_contiguous (n_extracted, MPI_FLOAT, &newType);
```

```
MPI_Type_commit(&newType);
```

```
if (rank == 0) {
```

```
    dest = 1;
```

```
    MPI_Send(&a[5], 1, newType, dest, tag, MPI_COMM_WORLD);
```

```
}
```

```
else if (rank == 1) {
```

```
    source = 0;
```

```
    MPI_Recv(b, n_extracted, MPI_FLOAT, source, tag, MPI_COMM_WORLD, &stat);
```

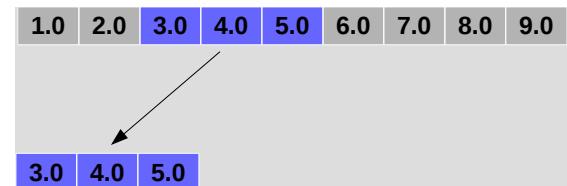
```
    for (i=0;i<n_extracted;++i) printf("On rank %d b[%d]= %2.1f \n", rank, i, b[i]);
```

```
}
```

```
    MPI_Type_free(&newType);
```

[...]

DdtContiguous1D.c



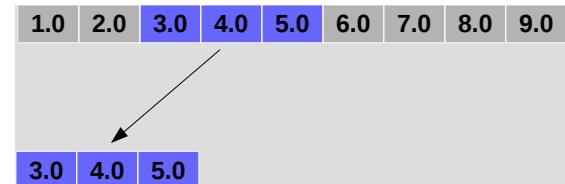
```
> mpirun -np 2 ./a.out  
On rank 1 b[0]= 6.0  
On rank 1 b[1]= 7.0  
On rank 1 b[2]= 8.0
```

# MPI\_Type\_contiguous

[...]

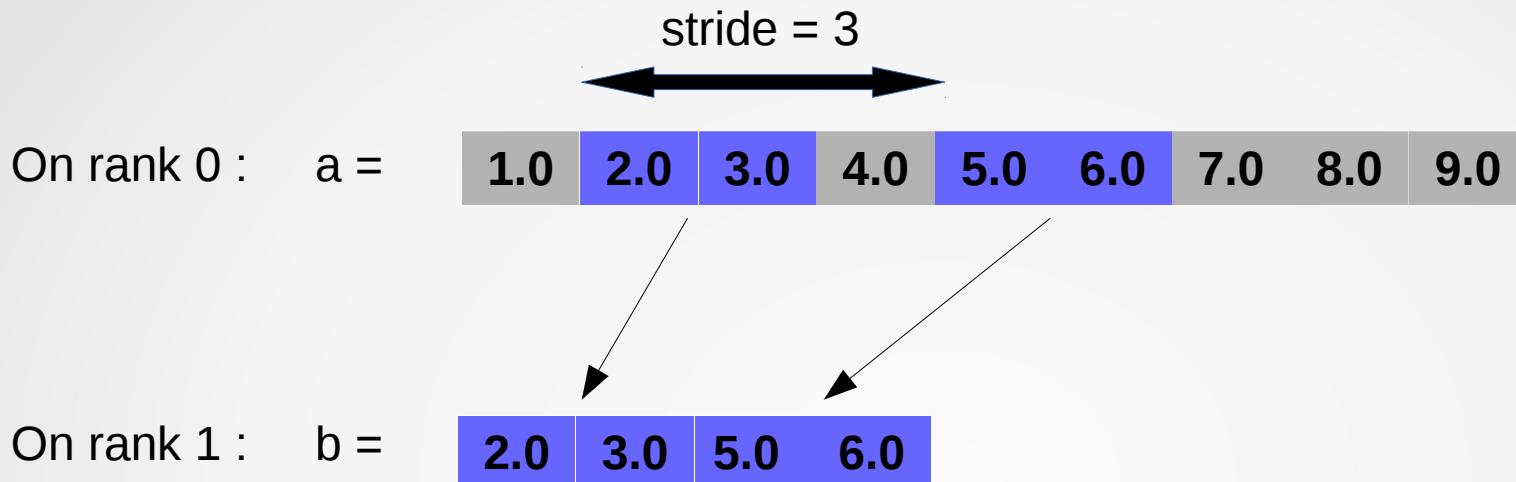
```
float a[9] = {1.0, 2.0, 3.0, 4.0, 5.0, 6.0, 7.0, 8.0, 9.0};  
int n_extracted = 3;  
float b[n_extracted];  
MPI_Datatype newType;  
MPI_Type_contiguous (n_extracted, MPI_FLOAT, &newType);  
MPI_Type_commit(&newType);                                ← commit required  
if (rank == 0) {  
    dest = 1;  
    MPI_Send(&a[2], 1, newType, dest, tag, MPI_COMM_WORLD);  
}  
else if (rank == 1) {  
    source = 0;  
    MPI_Recv(b, n_extracted, MPI_FLOAT, source, tag, MPI_COMM_WORLD, &stat);  
    for (i=0;i< n_extracted;++i) printf("On rank %d b[%d]= %2.1f \n", rank, i, b[i]);  
}  
MPI_Type_free(&newType);                                ← so that newType can be re-used  
[...]
```

DdtContiguous1D.c



```
> mpirun -np 2 ./a.out  
On rank 1 b[0]= 3.0  
On rank 1 b[1]= 4.0  
On rank 1 b[2]= 5.0
```

# MPI\_Type\_vector

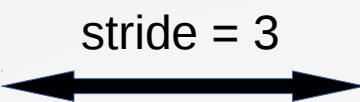


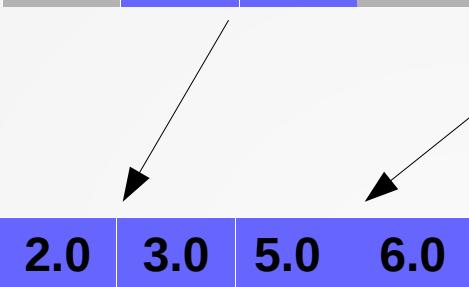
**MPI\_Type\_vector (n\_blocks, blocklength, stride, basictype, &*newtype*)**

C code

- **n\_blocks = 2**
  - **blocklength = 2**
  - **stride = 3**
  - **basicType = MPI\_FLOAT**
- "newType" generated

# MPI\_Type\_vector

On rank 0 : a =   
1.0 2.0 3.0 4.0 5.0 6.0 7.0 8.0 9.0

On rank 1 : b =   
2.0 3.0 5.0 6.0

1.0	2.0	3.0
4.0	5.0	6.0
7.0	8.0	9.0

"row major order"

# Matrices in C and Fortran

C:

```
float a[3][3] = {1.0, 2.0, 3.0, 4.0, 5.0, 6.0, 7.0, 8.0, 9.0};
```

C code

$$\xrightarrow{\hspace{1cm}} \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix}$$

"row major order"

Fortran:

```
real, dimension(3,3) :: A
```

```
a = reshape( (/ 1.0, 2.0, 3.0, 4.0, 5.0, 6.0, 7.0, 8.0, 9.0 /), (/ 3, 3 /) )
```

F90 code

$$\xrightarrow{\hspace{1cm}} \begin{bmatrix} 1 & 4 & 7 \\ 2 & 5 & 8 \\ 3 & 6 & 9 \end{bmatrix}$$

"column major order"

# Matrices in C and Fortran

C:

```
float a[3][3] = {1.0, 2.0, 3.0, 4.0, 5.0, 6.0, 7.0, 8.0, 9.0};
```

C code

$$\xrightarrow{\hspace{1cm}} \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix}$$

**MPI\_Type\_contiguous**  
extracts **rows**

Fortran:

```
real, dimension(3,3) :: A
```

```
a = reshape( (/ 1.0, 2.0, 3.0, 4.0, 5.0, 6.0, 7.0, 8.0, 9.0 /), (/ 3, 3 /) )
```

F90 code

$$\xrightarrow{\hspace{1cm}} \begin{bmatrix} 1 & 4 & 7 \\ 2 & 5 & 8 \\ 3 & 6 & 9 \end{bmatrix}$$

**MPI\_TYPE\_CONTIGUOUS**  
extracts **columns**

# Matrices in C and Fortran

C:

```
float a[3][3] = {1.0, 2.0, 3.0, 4.0, 5.0, 6.0, 7.0, 8.0, 9.0};
```

C code

$$\xrightarrow{\hspace{1cm}} \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix}$$

**MPI\_Type\_vector**  
extracts **columns**

Fortran:

```
real, dimension(3,3) :: A
```

```
a = reshape( (/ 1.0, 2.0, 3.0, 4.0, 5.0, 6.0, 7.0, 8.0, 9.0 /), (/ 3, 3 /) )
```

F90 code

$$\xrightarrow{\hspace{1cm}} \begin{bmatrix} 1 & 4 & 7 \\ 2 & 5 & 8 \\ 3 & 6 & 9 \end{bmatrix}$$

**MPI\_TYPE\_VECTOR**  
extracts **rows**

# Moreover...

C code

**MPI\_Type\_contiguous (n\_extracted, basicType, &newType)**

**MPI\_Type\_vector (n\_blocks, blocklength, stride, basicType, &newtype)**

**MPI\_Type\_indexed (n\_blocks, blocklengths[ ], offsets[ ], basicType, &newtype)**

**MPI\_Type\_struct (n\_blocks, blocklengths[ ], offsets[ ], basicTypes[ ], &newtype)**

# Layout

- Introduction & “Hello World”
- Point-to-point Communications
- Collective Communications
- Derived Data Types
- Communicators and Topologies
- Exercises

# Beyond MPI\_COMM\_WORLD...

There exists MPI statements to create and handle  
**communicators different from MPI\_COMM\_WORLD.**

→ enable for instance collective communications operations  
across a **subset** of tasks.

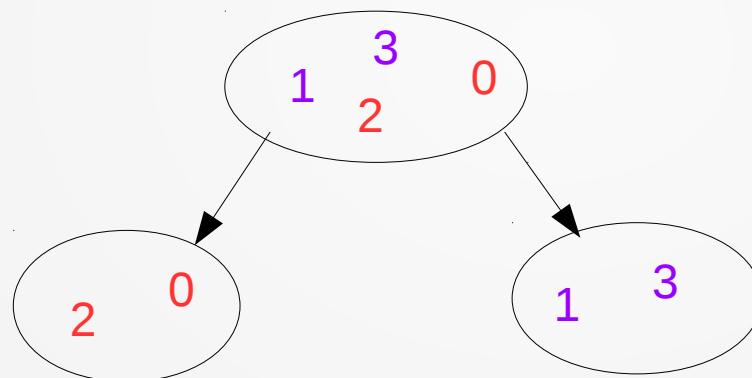
Ex : **MPI\_COMM\_SPLIT(comm, color, key, new\_comm)**  
partitions the communicator **comm** according to the value of **color**.  
→ new communicators **new\_comm** are created, each containing  
all the processes of the same color.

# MPI\_Comm\_split

`MPI_COMM_SPLIT(comm, color, key, new_comm)`

Example with 2 colors:

- `comm = MPI_COMM_WORLD`
- `color = 0` on **even** ranks and `color = 1` on **odd** ranks



NB : The same name `new_comm` then refers to different communicators on processes of different colors.

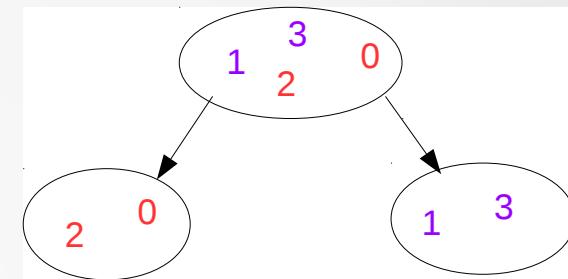
# Even/Odd Rank Split

[...]

```
int orig_rank, new_rank, color, key=0;  
MPI_Comm new_comm;  
MPI_Init (&argc, &argv);  
MPI_Comm_rank (MPI_COMM_WORLD, &orig_rank);  
color = orig_rank%2;  
MPI_Comm_split (MPI_COMM_WORLD, color, key, &new_comm);  
MPI_Comm_rank (new_comm, &new_rank);  
printf("orig_rank = %d color = %d new_rank = %d \n", orig_rank, color, new_rank);  
MPI_Comm_free (&new_comm);  
MPI_Finalize();
```

[...]

evenOddSplit.c



```
> mpirun -np 4 ./a.out  
orig_rank = 0 color = 0 new_rank = 0  
orig_rank = 1 color = 1 new_rank = 0  
orig_rank = 2 color = 0 new_rank = 1  
orig_rank = 3 color = 1 new_rank = 1
```

# Virtual topologies

Communicators can be defined to represent a topology, i.e., a mapping of MPI processes (i.e., MPI ranks) into a geometric pattern.

Here we consider cartesian topologies. Example:

2 (0,2)	5 (1,2)	8 (2,2)
1 (0,1)	4 (1,1)	7 (2,1)
0 (0,0)	3 (1,0)	6 (2,0)

Interest : provide tools to easily determine neighbors, correspondance between the rank and the coordinates in the grid.

Note : May not necessarily correspond to physical CPU layout  
→ « virtual ».

# Cartesian topologies

```
MPI_Cart_create(MPI_COMM_WORLD, ndims, dims, ..., &cart_comm)
```

→ creates a new communicator **cart\_comm** representing a cartesian topology in **ndims** dimensions, of size **dims**.

2 (0,2)	5 (1,2)	8 (2,2)
1 (0,1)	4 (1,1)	7 (2,1)
0 (0,0)	3 (1,0)	6 (2,0)

**ndims = 2**  
**dims = (3,3)**

# Coordinates from rank

**MPI\_Cart\_coords(cart\_comm, rank, ndims, coords)**

↓  
output

2 (0,2)	5 (1,2)	8 (2,2)
1 (0,1)	4 (1,1)	7 (2,1)
0 (0,0)	3 (1,0)	6 (2,0)

```
> mpirun -np 9 ./a.out | sort
rank= 0 → coords= 0 0
rank= 1 → coords= 0 1
rank= 2 → coords= 0 2
rank= 3 → coords= 1 0
[...]
rank= 8 → coords= 2 2
```

# Rank from coordinates

```
MPI_Cart_rank (cart_comm, coords, &the_rank);
```

↓  
output

2 (0,2)	5 (1,2)	8 (2,2)
1 (0,1)	4 (1,1)	7 (2,1)
0 (0,0)	3 (1,0)	6 (2,0)

```
> mpirun -np 9 ./a.out | sort  
coords= 1 2 → the_rank= 5
```

# Neighbors

**MPI\_Cart\_shift (cart2D\_comm, direction, displacement,  
&neighbors[...], &neighbors[...]);**

output

2 (0,2)	5 (1,2)	8 (2,2)
1 (0,1)	4 (1,1)	7 (2,1)
0 (0,0)	3 (1,0)	6 (2,0)

```
> mpirun -np 9 ./a.out | sort
rank= 0 → neighbors(w,e,s,n)= -2 3 -2 1
...
rank= 3 → neighbors(w,e,s,n)= 0 6 -2 4
rank= 4 → neighbors(w,e,s,n)= 1 7 3 5
...
rank= 8 → neighbors(w,e,s,n)= 5 -2 7 -2
```

# Automatic dimensioning

**MPI\_Dims\_create** ( ntasks, ndims, **dims**);

↓  
output

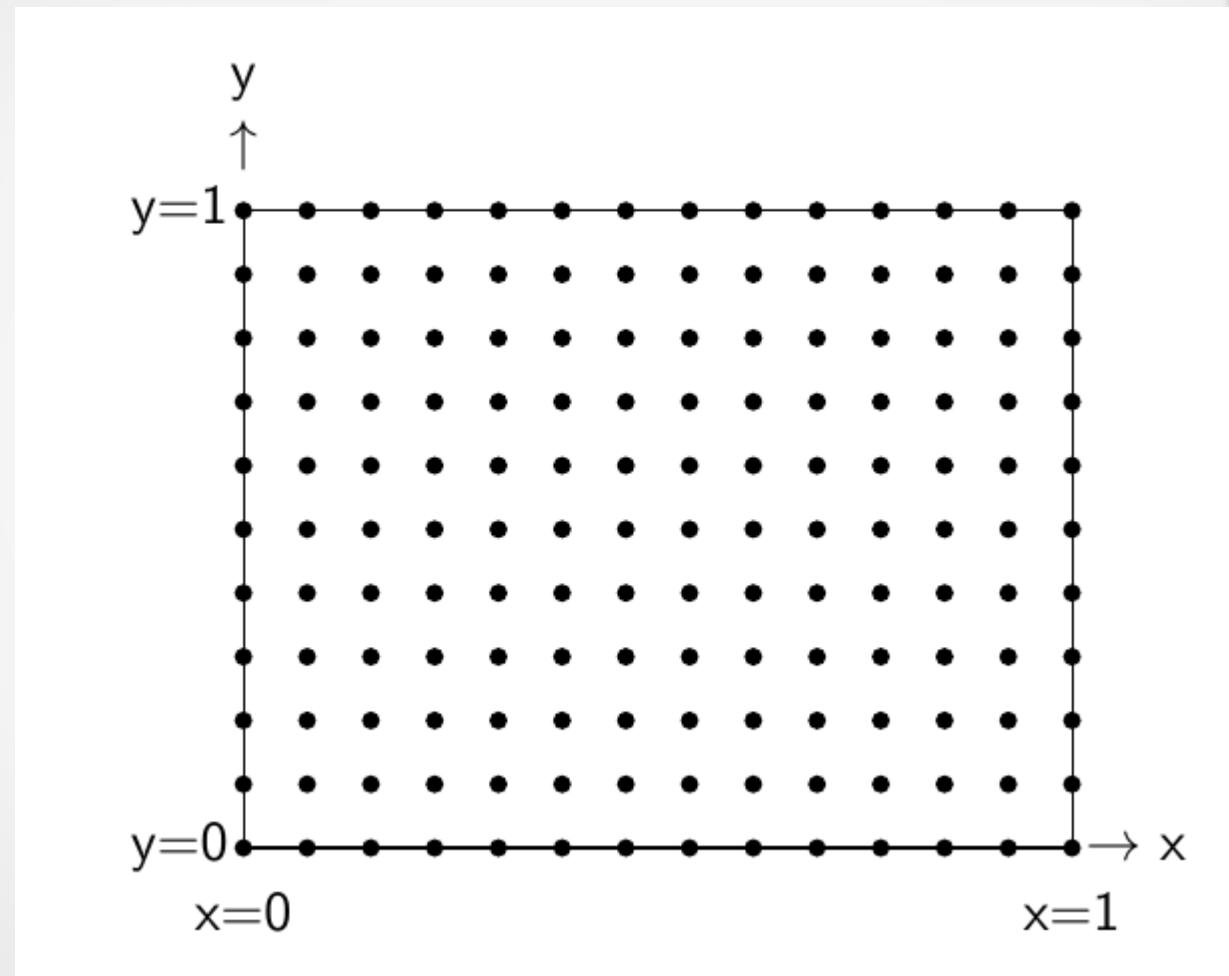
```
> mpirun -np 4 ./a.out  
dims[0]= 2 dims[1]= 2
```

```
> mpirun -np 6 ./a.out  
dims[0]= 3 dims[1]= 2
```

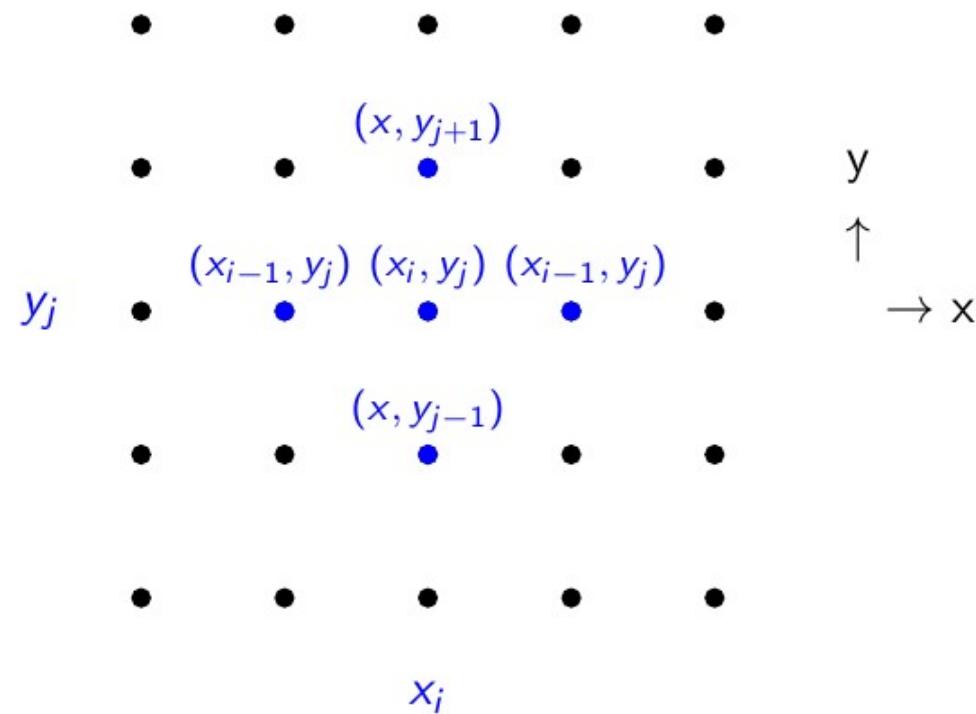
1 (0,1)	3 (1 ,1)
0 (0,0)	2 (1,0)

1 (0,1)	3 (1 ,1)	5 (2,1)
0 (0,0)	2 (1,0)	4 (2,0)

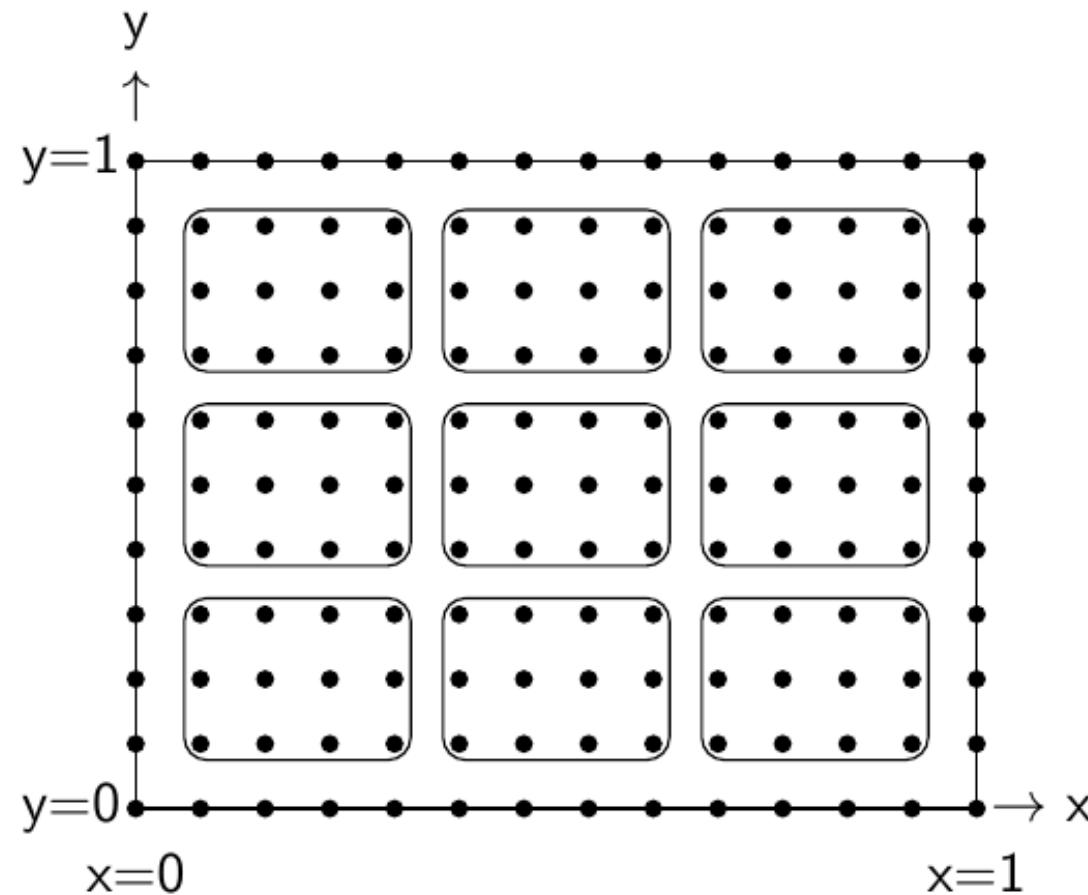
# Illustration: PDE on a finite difference grid



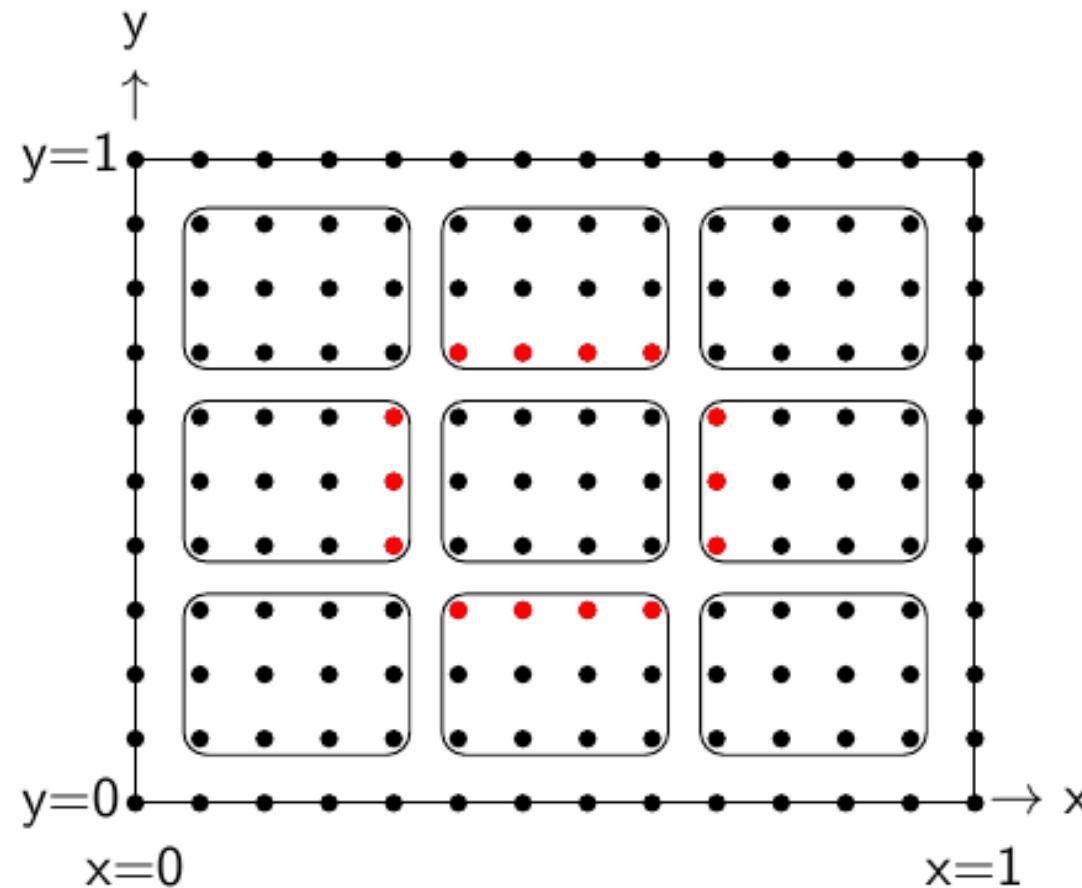
# 5-point finite difference scheme



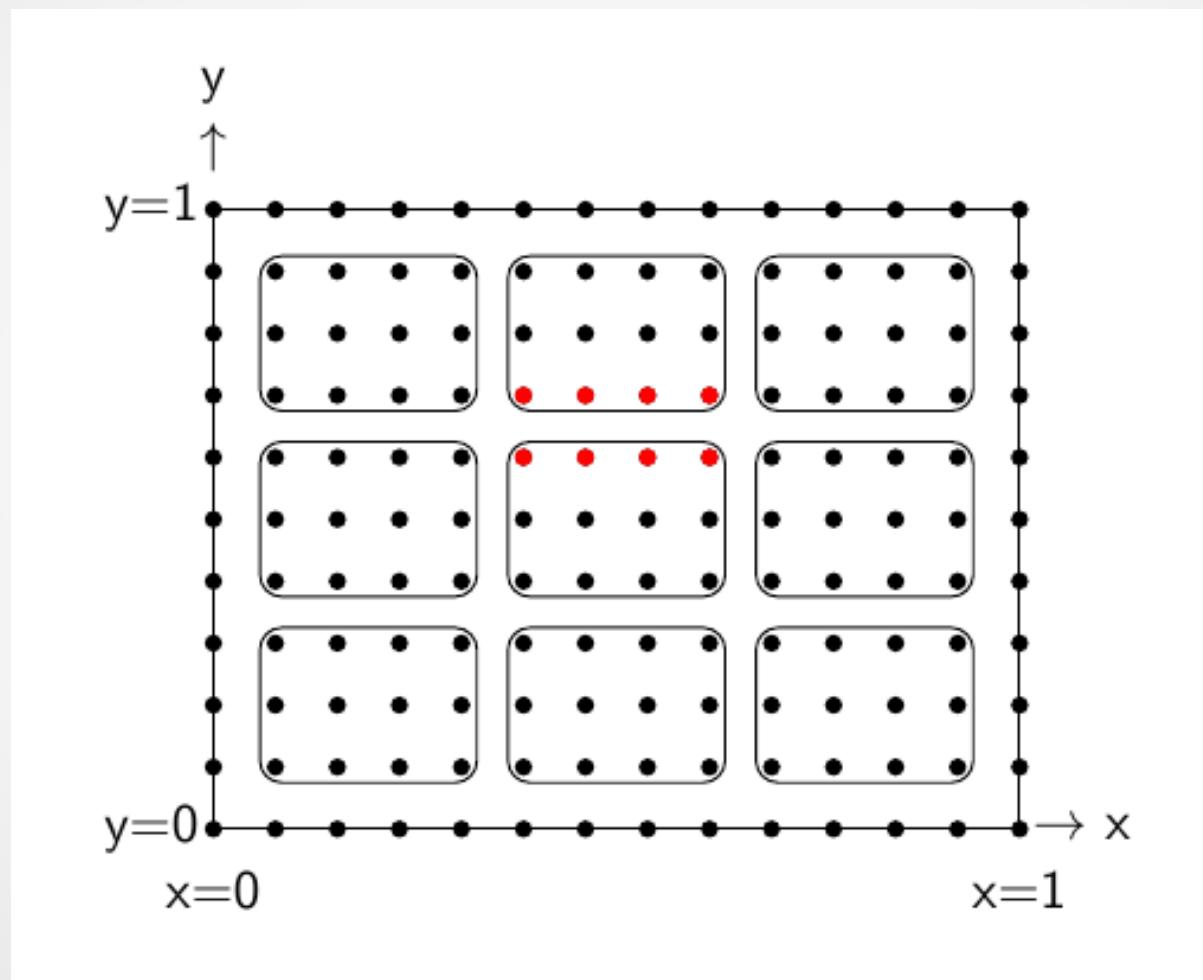
# Let ntasks = 9



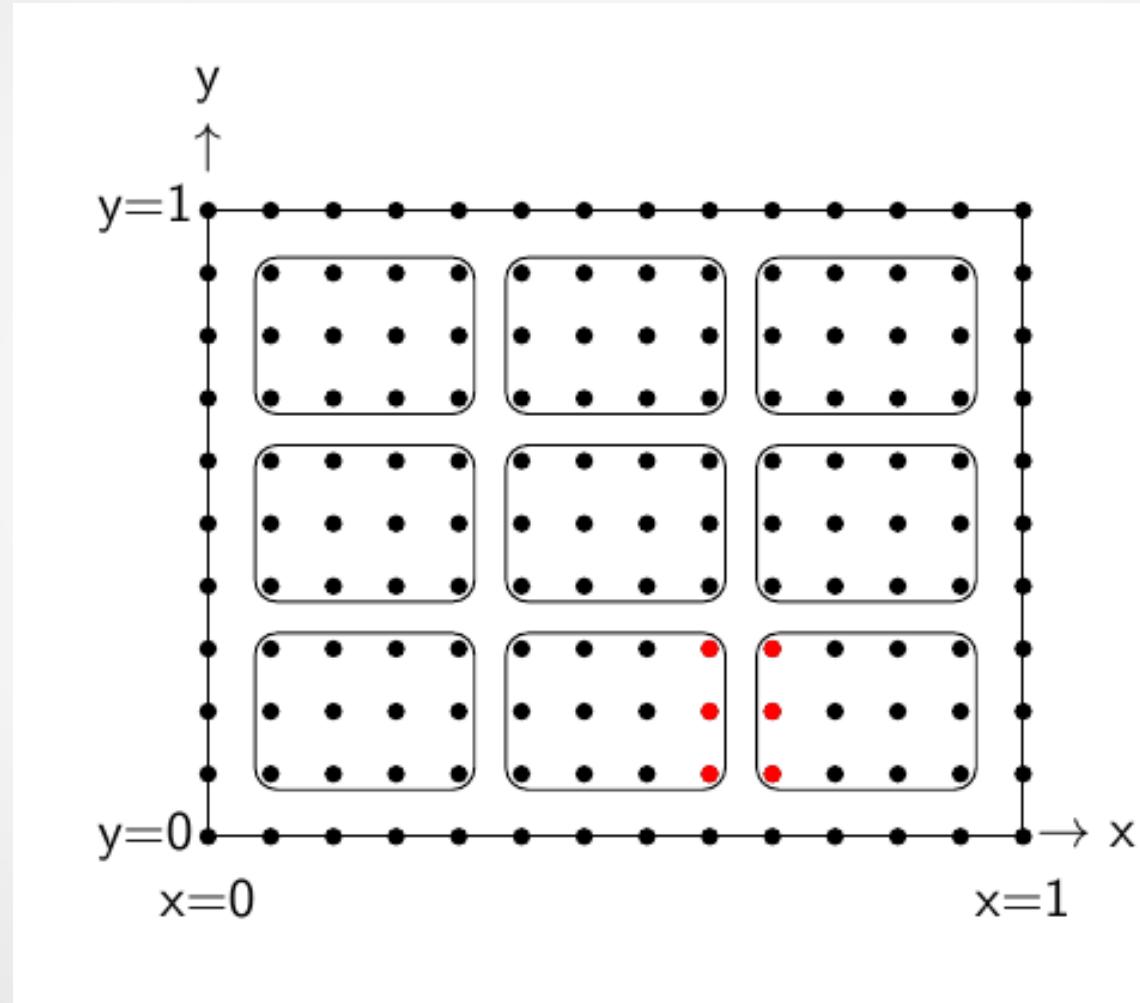
# Ghost points



# Exchanges needed...

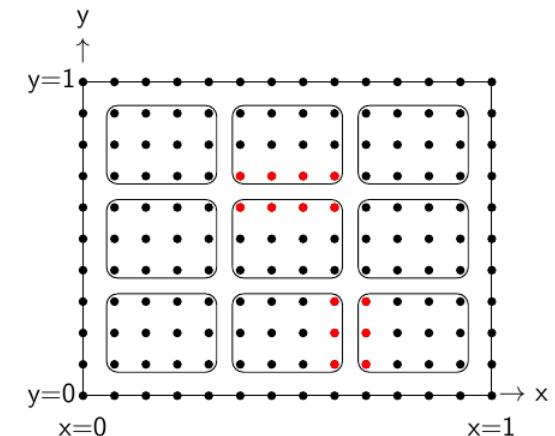


# Exchanges needed...



# Use cartesian topology! (and DDT)

- **MPI\_Cart\_create** → create topology
- **MPI\_Cart\_coords** → coordinates from rank
- **MPI\_Cart\_shift** → neighbors
- **Derived data types:**
  - “rowType” for North-South exchanges
  - “columnType” for East-West exchanges
- **MPI\_Dims\_create** for automatic dimensioning



# Numerical results on MeCS' uv100

Poisson equation, Gauss-Seidel Iteration.

Ncpus	200*200 mesh
1	32
2	16
4	8
8	4

Perfect scaling

*Times in seconds*

# Numerical results on MeCS' uv100

Poisson equation, Gauss-Seidel Iteration.

Ncpus	200*200 mesh
1	32
2	16
4	8
8	4
16	8

Perfect scaling

... but not above 8 cpus.

*Times in seconds*

# Numerical results on MeCS' uv100

Poisson equation, Gauss-Seidel Iteration.

Ncpus	200*200 mesh	800*800 mesh
<b>1</b>	32	
<b>2</b>	16	
<b>4</b>	8	
<b>8</b>	4	1052
<b>16</b>	8	524

*Times in seconds*

# Numerical results on MeCS' uv100

Poisson equation, Gauss-Seidel Iteration.

Ncpus	200*200 mesh	800*800 mesh
<b>1</b>	32	
<b>2</b>	16	
<b>4</b>	8	
<b>8</b>	4	1052
<b>16</b>	8	524
<b>32</b>		900

*Times in seconds*

## N.B.: In real life...

Don't program PDE solver from scratch on your own!

Use existing tools, like:  
PETSc, Trilinos, FeniCS, FreeFEM,...

# Exercises

# Exercise 1

- Compile and run the "Hello World" example on different numbers of processors by varying the -np argument. Have only a given MPI process (e.g. rank 0) print the "Hello World" message.
- Compile and run the given Send/Recv example **sendRecv.c/f90** on  $N = 2$  processors. See what happens when launching on  $N \neq 2$  processors. Modify the code to have the integer 2 sent instead of the letter 'B' from rank 0 to rank 1.

## Exercise 2

Write a MPI code such that each process exchanges its rank with its "partner" whose rank is defined as:

$$\text{partner\_rank} = \text{ntasks} - (\text{rank}+1)$$

Have each MPI process print the integer it receives to check that it corresponds to the rank of its partner.

```
> mpirun -np 3 ./a.out
Rank 0 has partner rank 2
Rank 1 has partner rank 1
Rank 2 has partner rank 0
Integer received by rank 1 : 1
Integer received by rank 0 : 2
Integer received by rank 2 : 0
```

# Exercise 3

From D. Lecas et al. (IDRIS)

[http://www.idris.fr/data/cours/parallel/mpi/choix\\_doc.html](http://www.idris.fr/data/cours/parallel/mpi/choix_doc.html)

The **coinTossSerial.c** program (next slide) simulates coin tossing (« pile ou face ») on one processor.

From there, write a parallel program that simulates simultaneous coin tossing on different MPI processes.

Then, build a program that observes toss results on all the MPI processes, and repeats the simultaneous coin tossing until unanimity is reached or until a given number of maximum attempts is reached.

# Exercise 3

```
#include <stdio.h>
#include <stdlib.h>
#include <time.h>
int main(int argc, char *argv[])
{
    int tossResult;

    srand(time(NULL));
    tossResult = (int) ((double)rand() / ((double)RAND_MAX + 1) * 2) ;
    // tossResult = 0 or 1

    printf("tossResult=%d \n", tossResult);
}
```

coinTossSerial.c

# Exercise 3

```
program main
! use mpi
implicit none
include 'mpif.h'
integer :: tossResult, K
integer, dimension(8) :: timeValues
real :: random
call date_and_time(values=timeValues)
call random_seed(size=K)
call random_seed(put=timeValues(1:K))
call random_number(random)
tossResult = nint(random)
write(*,*) 'tossResult = ', tossResult
end
```

coinTossSerial.f90